Image Compression EE274, Fall22

Image Compression



764x512x3 bytes = 1.1MB! (Uncompressed)

Image Compression -> JPEG 40x



Uncompressed -> 1.1MB JPEG -> 27KB (~40x!)

Image Compression -> JPEG 80x



Uncompressed -> 1.1MB JPEG -> 14KB (~80x!)

Image Compression -> JPEG 137x



Uncompressed -> 1.1MB JPEG -> 8KB (~137x!)

Image Compression -> BPG



Uncompressed -> 1.1MB BPG -> 8KB (~137x!)

HiFiC -> ML-based image compression



Uncompressed -> 1.1MB BPG -> 8KB (~137x!)

Lossy Compression

Incredible performance gains! ~40x-137x gains without much noticeable difference (depending upon the codec)

So ubiquitous, my DSLR camera does JPEG compression by default :-| ..
(difficult to find a "dataset" of non-compressed images)

JPEG, JPEG2000, BPG (HEIC), AVIF, JPEG-XL, ML-based image compressors …

Exploiting Spatial correlation in the data

Key Idea -> We need to somehow exploit/remove the correlation between neighboring pixels.









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TRANSFORM CODING!

Transform Coding -> RECAP



Block Transform Coding



Linear Transform Coding



$$\mathbf{x} = \mathbf{A}^{-1}\mathbf{y} = \mathbf{A}^{\mathrm{T}}\mathbf{y}$$

Block Transform Coding

Step 1 -> Cut the image into blocks (eg 8x8), [grayscale]

X



KLT -> Transform Coding

Step 1 -> Cut the image into blocks X(eg 8x8) Step 2 -> Find the transform matrix A using Karhunen-Loeve Transform (KLT)









KLT -> Transform Coding

- Decorrelation by design: Decorrelated transform coefficients
- Depends upon the data: Transform depends upon the input image
- Slow: Non-structured matrix of size NxN = 64x64, matrix multiplication is N^2 (too slow :(), KLT construction is also slow

Q: Can we design a structured transform, which is close to optimal? (i.e. to the KLT matrix)



- 1D-> Discrete Cosine transform
 - = values of the cosine function at different quantized values
- Forms the basis of any input of size 5
- The DCT vectors are orthonormal

$$X_k = \sum_{n=0}^{N-1} x_n \cos\left[\frac{(2n+1)\pi k}{2N}\right] \iff X_k = \vec{C}_k^T \vec{x}$$



Transform Coding -> 1D-DCT- examples



Transform Coding -> 1D-DCT- examples







2D-DCT basis vectors (apply 1D along x, and then y)

		1	2	3	4	5	6	7	8	9	
								8	а.	Ο.	
A		0.000	0.000	1.000	0.000	0.000	0.000	0.000	0.000	0.000	
в		0.667	0.000	0.000	-0.333	0.000	0.000	0.000	0.000	0.000	
с		0.400	0.000	0.693	0.000	0.000	-0.200	0.000	0.000	0.000	
D	н	0.300	0.173	0.693	-0.100	0.000	-0.200	0.000	0.000	0.000	
E	5	0.200	-0.065	0.064	0.435	-0.527	0.041	-0.547	-0.267	-0.014	
F	5	0.200	-0.065	0.064	0.435	-0.527	0.041	-0.547	-0.267	0.000	

Transform Coding -> 2D-DCT vectors



2D-DCT basis vectors for 8x8 blocks















DCT -> Sparse



DCT -> Sparse



DCT -> Sparse (but higher frequencies)

Transform Coding -> DCT of noise



DCT -> Not-so sparse

- Observation: For most of the "natural" image blocks, the DCT is sparse, and concentrated in the lower frequencies





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- Energy Compaction: Most of the high-frequency DCT coefficients have low magnitude, so can be ignored during lossy-compression (i.e. perform lowpass filtering)

This key observation forms the basis of JPEG image compression

JPEG Image Compression







A photo of a European wildcat with the compression rate decreasing and hence quality increasing, from left to right

Ella manuela								
extension	.]pg, .]peg,							
extendion	. jpe							
	.jit, .jtit,							
	.jfi							
Internet	image/jpeg							
media type								
Type code	JPEG							
Uniform Type	public.jpeg							
Identifier (UTI)								
Magic number	ff d8 ff							
Developed by	Joint Photographic							
	Experts Group, IBM, Mitsubishi Electric, AT&T, Canon Inc. ^[1]							
Initial release	September 18, 1992; 30							
	years ago							
Type of format	Lossy image compression							
	format							
Standard	ISO/IEC 10918, ITU-T							
	T.81, ITU-T T.83, ITU-T							
	T.84, ITU-T T.86							
Website	www.ipeg.org/ipeg/s							
	THILD G. O'G' D'G' L							

JPEG Image Compression



Optional color transform + color sub-sampling
RGB colorspace



YCbCr Color space



Y = 0.299 * R + 0.587 * G + 0.114 * B

Cr = 0.500 * R - 0.419 * G - 0.081 * B

Optional color transform + color sub-sampling



JPEG Image Compression (Baseline Encoding)



Optional color transform + color sub-sampling



Encoding done per channel (independently)

JPEG Image Compression -> 2D-Block DCT

- STEP-1: Cut the image into blocks of size 8x8

Input 8x8 block

221	218	211	196	189	189	174	149
230	220	223	205	193	188	177	160
197	183	175	185	193	198	200	193
183	183	168	170	151	129	139	166
183	185	175	181	163	187	126	154
192							
1/2	169	170	183	188	185	153	120
205	169 215	170 186	183 126	188 123	185 142	153 118	120 93

- STEP-1: Cut the image into blocks of size 8x8
- STEP-1.5: subtract 128, to center the pixels
- STEP-2: 2D-DCT of each 8x8 block

93	90	83	68	61	61	46	21
02	92	95	77	65	60	49	32
9	55	47	57	65	70	72	65
55	55	40	42	23	1	11	38
55	57	47	53	35	59	-2	26
64	41	42	55	60	57	25	-8
7	87	58	-2	-5	14	-10	-35
38	14	33	33	-21	-23	-43	-34



338	145	-8	18	-7	4	16	-14
162	-41	3	2	3	-1	-13	9
-17	57	-2	-2	-20	16	2	10
41	19	-24	31	-19	-8	4	-1
-59	7	-2	-32	21	-1	6	-15
-19	12	32	0	-16	-9	-15	12
7	-55	-24	17	20	15	-4	0
15	-11	10	11	-18	-13	10	-10

2D DCT

Input 8x8 block (zero centered)



Input 8x8 block (zero centered) 1D DCT (along x)



Input 8x8 block (zero centered)

2D DCT

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2D DCT



2D basis vectors



JPEG Image Compression -> Quantization

- STEP-1: Cut the image into blocks of size 8x8
- STEP-2: 2D-DCT of each 8x8 block
- STEP-3: uniform scalar quantize DCT coefficients based on the quantization table.



JPEG Image Compression -> Quantization

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JPEG Image Compression -> Quantization

16	11	10	16	24	40	51	61
12	12	14	19	26	58	60	55
14	13	16	24	40	57	69	56
14	17	22	29	51	87	80	62
18	22	37	56	68	109	103	77
24	35	55	64	81	104	113	92
49	64	78	87	103	121	120	101
72	92	95	98	112	100	103	99

6	4	4	6	10	16	20	24
5	5	6	8	10	23	24	22
6	5	6	10	16	23	28	22
6	7	9	12	20	35	32	25
7	9	15	22	27	44	41	31
10	14	22	26	32	42	45	37
20	26	31	35	41	48	48	40
29	37	38	39	45	40	41	40

Quality factor: 50

Quality factor: 80



For different compression rate

90	-40	0	4	0	0	0	0
0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
11	-3	0	0	0	0	0	0
11 0	-3 0	0 0	0 0	0 0	0 0	0 0	0 0
11 0 0	-3 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0

Quantized, transformed Coefficients for one 8x8 block Q: How would you go ahead with lossless compression of these coefficients?



Quantized, transformed Coefficients for one 8x8 block

JPEG Image Compression -> Entropy coding

90	-40	0	4	0	0	0	0
0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
11	-3	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

JPEG Specific Huffman Encoding

It's quite complicated

- ${\scriptstyle \bullet \rm Signs}$ of coefficients
- •All 8 \times 8 blocks
- Top left (DC) coefficients encoded separately from other (AC) coefficients

 $ig\{$ [(0, 7), 90], [(0, 6), -40], [(1, 3), 5], [(2, 3), 4], [(3, 4), 11], [(8, 2), -3], [(0, 0)] ig\}



JPEG Compression:

- Color Channels: For Each color channel is encoded independently of each other
- Block Coding: JPEG encodes each 8x8 almost independently (except the DC coefficient).
- Huffman/Arithmetic: JPEG also has support for using Arithmetic coding, but is rarely used.

Linear Transform Coding



Image Compression -> Analysis



JPEG Decoder specification



JPEG Decoder specification

Common JPEG markers ^[48]				
Short name	Bytes	Payload	Name	Comments
SOI	0xFF, 0xD8	none	Start Of Image	
SOF0	0xFF, 0xC0	variable size	Start Of Frame (baseline DCT)	Indicates that this is a baseline DCT-based JPEG, and specifies the width, height, number of components, and component subsampling (e.g., 4:2:0).
SOF2	0xFF, 0xC2	variable size	Start Of Frame (progressive DCT)	Indicates that this is a progressive DCT-based JPEG, and specifies the width, height, number of components, and component subsampling (e.g., 4:2:0).
DHT	0xFF, 0xC4	variable size	Define Huffman Table(s)	Specifies one or more Huffman tables.
DQT	0xFF, 0xDB	variable size	Define Quantization Table(s)	Specifies one or more quantization tables.
DRI	0xFF, 0xDD	4 bytes	Define Restart Interval	Specifies the interval between RST <i>n</i> markers, in Minimum Coded Units (MCUs). This marker is followed by two bytes indicating the fixed size so it can be treated like any other variable size segment.
SOS	0xFF, 0xDA	variable size	Start Of Scan	Begins a top-to-bottom scan of the image. In baseline DCT JPEG images, there is generally a single scan. Progressive DCT JPEG images usually contain multiple scans. This marker specifies which slice of data it will contain, and is immediately followed by entropy-coded data.
RSTn	0xFF, 0xD <i>n</i> (<i>n</i> =07)	none	Restart	Inserted every <i>r</i> macroblocks, where <i>r</i> is the restart interval set by a DRI marker. Not used if there was no DRI marker. The low three bits of the marker code cycle in value from 0 to 7.
APP <i>n</i>	0xFF, 0xE <i>n</i>	variable size	Application-specific	For example, an Exif JPEG file uses an APP1 marker to store metadata, laid out in a structure based closely on TIFF.
СОМ	0xFF, 0xFE	variable size	Comment	Contains a text comment.
EOI	0xFF, 0xD9	none	End Of Image	

What are the issues with JPEG?

- Block size 8x8



What are the issues with JPEG?

- Block size 8x8
- Blocks processed independently



What are the issues with JPEG?

- Block size 8x8
- Blocks processed independently
- lossless coding can be improved



Image Compression -> JPEG 137x



Uncompressed -> 1.1MB JPEG -> 8KB (~137x!)

Image from Kodak dataset

Image Compression -> BPG



Uncompressed -> 1.1MB BPG -> 8KB (~137x!)

Image from Kodak dataset

Larger blocks are allowed (64x64), (32x32)





Larger blocks are allowed (64x64), (32x32)



Fig. 3.4 Example for the partitioning of a 64×64 coding tree unit (CTU) into coding units (CUs) of 8×8 to 32×32 luma samples. The partitioning can be described by a quadtree, also referred to as coding tree, which is shown on the *right*. The numbers indicate the coding order of the CUs

Larger blocks are allowed



Predictive coding -> BPG/H.265



Predictive coding -> BPG/H.265

Predict next block, based on previously encoded blocks



BPG Prediction modes





- For simplicity (and speed) you only use the border pixels of the encoded blocks to predict the next block.
- Try multiple models, and use whichever works best
BPG Prediction modes



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- Try multiple models, and use whichever works best

BPG Predictive coding

Blocks are not independent anymore! Predictive coding



BPG Predictive coding

Blocks are not independent anymore! Predictive coding



BPG Predictive coding

Blocks are not independent anymore! Predictive coding



- Exploits correlation between blocks: Predictive coding
- Use larger transform blocks: Better energy compaction, better compression
- CABAC instead of Huffman: Adaptive Arithmetic coding instead of Huffman.

BPG -> CABAC



Fig. 8.1 CABAC block diagram (from the encoder perspective): Binarization, context modeling (including probability estimation and assignment), and binary arithmetic coding. In *red*: Potential throughput bottlenecks, as further discussed from the decoder perspective in Sect. 8.3.2

Image Compression -> JPEG 137x



Uncompressed -> 1.1MB JPEG -> 8KB (~137x!)

Image from Kodak dataset

Image Compression -> BPG



Uncompressed -> 1.1MB BPG -> 8KB (~137x!)

Image from Kodak dataset

What next?

- Beyond Linear transform: JPEG/JPEG2000/BPG all use variants of DCT, DWT etc. can we obtain better performance with non-linear transforms
- End-to-End RD Optimization: JPEG the R-D optimization is not accurate. Rate needs to be shared between different channels etc. Can we make that end-to-end?

https://wave-one.github.io/iframe_comparisons/

Questions?